

Algebra II

12-7

Law of Sines

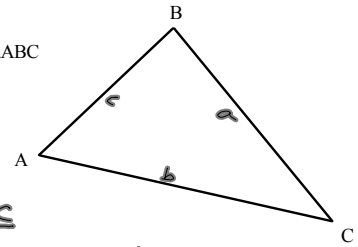
Law of Sines -

Given a general triangle $\triangle ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

or

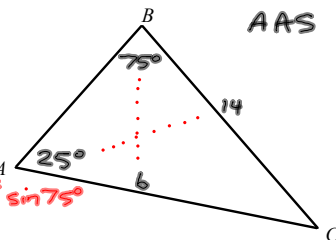
$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$



Works two types of triangles:
AAS (ASA)
ASS

Find the indicated part of $\triangle ABC$ to three significant digits or to the nearest tenth of a degree. If there are two solutions, give both. (pg 588)

- 1) $a=14$
 $\angle A = 25^\circ$
 $\angle B = 75^\circ$
 $b = \underline{32.0}$



AAS

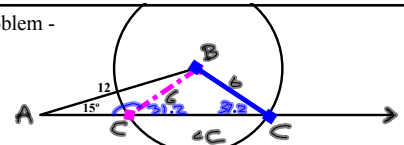
$$\frac{b}{\sin 75^\circ} = \frac{14}{\sin 25^\circ}$$

$$b = \frac{14 \sin 75^\circ}{\sin 25^\circ}$$

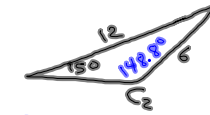
$$b = 31.998$$

The Angle Side Side problem -

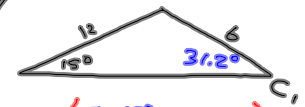
- $a=6$
 $c=12$
 $A=15^\circ$
 $\angle C = \underline{31.2^\circ}$ or $\underline{148.8^\circ}$



Both of the radii form feasible triangles, so in this case, there are two appropriate angle C answers.



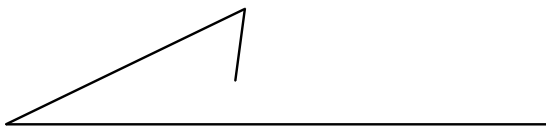
$$C_2 = 180 - C_1$$



$$\left(\frac{\sin 15^\circ}{6} = \frac{\sin C_1}{12} \right) 12$$

$$2 \sin 15^\circ = \sin C_1$$

$$\sin^{-1}(0.5176) \approx C_1 = 31.17$$



The ASS problem -

- If the side opposite is shorter than the side adjacent,
- No Solution (calculator error)
 - One Solution (right angle)
 - Two Solutions (calculator gives one, you find the other)

Pg 588

1-12 all

Pg 589

1-12 all (wp)